
CONVOLUTION PROBLEMS IN TIME-RESOLVED X-RAY DIFFRACTION

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Convolution problems in the time-resolved scattering of 10–1000-ps x-ray pulses are studied theoretically. The model system is a diluted solution of diatomic molecules A_2 dissolved in an inert solvent. This system is submitted to a sub-picosecond laser pulse, which promotes the molecules A_2 into an excited electronic state. The molecule then return into their ground state, passing through several intermediate electronic states. The effects of the finite duration of probing x-ray pulses on various x-ray signals are then examined in the frame of this model. Unbiased signals generated by very short x-ray pulses are explored first. Variations of a molecular geometry during this process are clearly visible in r -resolved, but are less explicit in q -resolved signals. The signals measured with x-ray pulses of a finite duration are studied next. Atomic motions remain detectable, but only if the x-ray pulses are shorter than or comparable to the times of a molecular dynamics. Here again, the r -resolved signals are more appropriate for monitoring the molecular dynamics than q -resolved signals. Finally, the effect of the insufficient temporal location of probing x-ray pulses with respect to that of exciting laser pulses is examined. It is shown that this last effect can be accounted for by simply replacing the true x-ray pulse intensity by another theoretically predicted intensity. The similarity of deconvolution techniques in spectroscopy and in time-resolved x-ray diffraction is strongly emphasized.

1. Introduction

The distortion of signals recorded due to imperfect recording devices is omnipresent in experimental sciences. This is particularly well known in optical spectroscopy, where spectral lines are deformed by the finite slit width of a spectrometer. This deformation may be large enough to compromise the interpretation of the observed data. It is thus particularly important to eliminate these errors, which can be done employing a technique called deconvolution (as for linear and modern nonlinear techniques in this field, see [1]). For the recent publications in this area, see [2–4].

Similar problems are also present in other fields of experimental sciences such as astrophysics, geophysics, chemical analysis by electronic spectroscopy, and cell biology. Somewhat surprisingly, the deconvolution tech-

niques are also useful to improve the quality of optical images. For example, the quality of a camera may be improved, at a given cost of optical elements, by incorporating appropriate deconvolution devices [1]. Another example is the Hubble space telescope, where the initial flaws of its mirror were partially corrected using the deconvolution techniques [1]. The deconvolution problems are thus omnipresent in experimental sciences.

It is then not too surprising that they also occur in time-resolved x-ray diffraction and absorption. For some reviews covering this field, see [5–7]. However, here they are not related to a finite slit width of spectrometers, but to a finite duration of probing x-ray pulses. The latter are generated by large scale instruments such as synchrotrons or linear accelerators with free electron lasers. Many questions can be asked, and the purpose of this paper is to answer some of them. How does a finite duration of x-ray pulses deform the experimental time-resolved x-ray signals? Which artifacts appear when these pulses are too long? How can the deconvolution problems in x-ray and in spectroscopic experiments be compared? In what follows, these questions will be examined theoretically. The similarity of the deconvolution techniques in x-ray physics and in spectroscopy is emphasized.

2. Basic Considerations

(A) The experiments under consideration are time-resolved x-ray diffraction experiments (Fig. 1). The liquid under consideration is pumped by a laser, which promotes a fraction of molecules into an excited quantum state. The further behavior of this system is probed using a series of time-delayed x-ray pulses. In liquids and disordered systems, the resulting diffraction patterns consist of circular rings centered on the forward beam. If a reaction takes place, these diffraction patterns vary with time. A collection of experimentally measured x-ray patterns can be transformed into a collection of molecular photographs by the Fourier sine transforma-

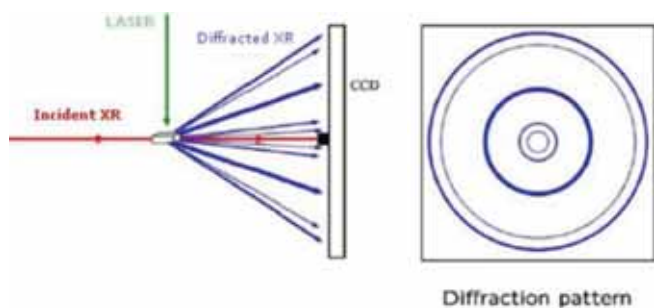


Fig. 1. Schematic representations of the experimental set-up (left) and the observed x-ray diffraction pattern (right)

tion. Atomic motions during a chemical reaction can be filmed by proceeding in this way.

(B) The central equation relating the measured x-ray signal $\Delta S(q, \tau)$, the true x-ray signal $\Delta S_{\text{inst}}(q, t)$ free of any distortion, and the x-ray pulse intensity $I_x(t)$ has the form of a convolution integral. First proposed intuitively [8] and later proven theoretically [9, 10], it reads

$$\Delta S(q, \tau) = \int dt I_x(t - \tau) \Delta S_{\text{inst}}(q, t). \quad (1)$$

Here, the signal $\Delta S(q, \tau) = S(q, \tau) - S(q)_{\text{eq}}$ describes the energy flux $S(q, \tau)$ of the diffracted x-ray radiation scattered in a solid angle in the presence of a pump minus the equivalent quantity $S(q)_{\text{eq}}$ in the absence of a pump, q is the scattering wave vector, and τ is the time elapsed between the pumping optical and probing x-ray pulses. The signal $\Delta S_{\text{inst}}(q, t) = S_{\text{inst}}(q, t) - S(q)_{\text{eq}}$ is defined similarly, except that the incident x-ray pulse is assumed to be infinitely short. The important signal $\Delta S_{\text{inst}}(q, t)$ cannot be measured, unfortunately, directly. It can be deduced from the experimental $\Delta S[q, \tau]$ by deconvolution (compare with Eq. (1)). One is thus faced with the same problem as spectroscopists, although not for the same reason.

(C) The measured signals $\Delta S(q, \tau)$, $\Delta S_{\text{inst}}(q, t)$ are not related to a molecular geometry directly, and the Fourier transformation of these signals is necessary. This statement is valid under static and quasistatic conditions. It is thus useful to introduce the quantities

$$\begin{aligned} \Delta S[r, \tau] &= 1/2\pi^2 r \int dq q M(q) \Delta S(q, \tau) \sin(qr), \\ \Delta S_{\text{inst}}[r, t] &= 1/2\pi^2 r \int dq q M(q) \Delta S_{\text{inst}}(q, t) \sin(qr). \end{aligned} \quad (2)$$

The function $\Delta S_{\text{inst}}[r, t]$ is a linear combination of the atom-atom distribution functions $g_{ij}(r, t)$ [11], which in-

dicate the probability to find atoms i and j at a distance r at time t . The quantity $\Delta S_{\text{inst}}[r, t]$ is related to the geometry of the system and the atomic motion in films during a chemical reaction. Only if the molecular motions are slow as compared with the x-ray pulse, the signal $\Delta S[r, \tau]$ can be assimilated to $\Delta S_{\text{inst}}[r, t]$. If not, a finite pulse duration blurs molecular films noticeably.

(D) In order to connect the present x-ray study to more familiar optical studies, it seems useful to present the terminology used in convolution theory [1]. The convolution integral is generally written in the form $i(x) = \int dx' s(x - x') o(x')$, where $i(x)$ is called “intensity”, $s(x - x')$ is the “point spread function,” and $o(x')$ is an “object”. In spectroscopy, x, x' are frequencies ω, ω' , $i(x)$ is the observed band intensity $I(\omega)$, $s(x - x')$ is the apparatus function, and $o(x)$ the true band intensity $J(\omega')$. In time-resolved x-ray diffraction, x and x' are times τ and t , $i(x)$ are the observed diffraction signals $\Delta S(q, \tau)$ or $\Delta S[r, t]$, $s(x - x')$ is the x-ray beam intensity $I_x(t - \tau)$, and $o(x)$ are the true x-ray signals $\Delta S_{\text{inst}}(q, t)$ or $\Delta S_{\text{inst}}[r, t]$. These notions should be kept in mind to compare the deconvolution problems in spectroscopy and in x-ray diffraction.

3. Model System

A. As the purpose of the present paper is to study spurious effects from insufficiently short synchrotron pulses, our attention will be focused on events occurring between 1 and 100 ps. We thus decided to examine fast processes taking place, when a diluted solution of diatomic molecules A_2 is excited by a laser. It is sufficient in reality to study the contribution to the x-ray signal due to the solute molecule A_2 alone. In fact, there exist the procedures allowing one to eliminate the solvent part in the measured x-ray signal experimentally [12]. What remains is proportional to a weighted sum of terms associated with the atom pairs $AA, AB, AC\dots$, where A denotes the solute atoms and $B, C\dots$ stand for the solvent atoms. As these contributions usually peak in separate regions of the r -space, the signal of the AA pair can often be isolated. Note that $\Delta S_{\text{inst}}[r, t]$ is then simply proportional to the AA pair distribution function, $g_{AA}(r, t)$.

B. Our model is inspired by laser spectroscopy of halogen diatomics [13–15] and can be described as follows. The states X and Y of the dissolved molecule A_2 are attractive, whereas the state Z is repulsive (Fig. 2). The equilibrium A – A distances are r_X and r_Y in the states

X and Y . From the other side, the potential energy curves of the electronic states Y and Z are assumed to cross each other at a distance $r_Y + \Delta r_Y$. A molecule A_2 is submitted to an ultrafast laser pulse, which brings it to the repulsive state Z . The transition is supposed to be vertical, according to the Franck–Condon principle. Very rapidly, almost instantaneously, a laser-excited molecule reaches the crossing point $r_Y + \Delta r_Y$, where it switches from the state Z to the state Y ; two processes follow. The first of them is the passage of atoms A in the state Y of A_2 from its extended configuration $r_Y + \Delta r_Y$ to its equilibrium configuration r_Y . It is accomplished in a time τ_v of the order of 100 ps. The second process is the deexcitation of A_2 from the electronic state Y to the ground electronic state X . It is much slower and is realized in times τ_p of the order of 1000 ps.

C. This model is now described theoretically. Let $g_X(r, t)$ and $g_Y(r, t)$ denote the A – A atom distribution functions in the electronic states X and Y , $g_{eq}(r)$ the A – A distribution function in equilibrium conditions, $n_X(t)$ and $n_Y(t)$ fractional populations of these two electronic states, V the volume of the solution, and P a factor depending on the geometry of the experimental set-up. The following expressions then describe our model:

$$\Delta S_{\text{inst}}[r, t] = (e^2/mc^2) (P/V) \times \\ \times \{n_X(t)g_X(r, t) + n_Y(t)g_Y(r, t) - g_{eq}(r)\}, \quad (3)$$

$$g_X(r, t) = g_{eq}(r) = A \exp[-a_X(r - r_X)^2],$$

$$g_Y(r, t) = B \exp[-a_Y(r - r_Y - \Delta r_Y \exp(-t/\tau_v))^2], \quad (4)$$

$$n_X(t) = 1 - n_0 e^{-t/\tau_p}; \quad n_Y(t) = n_0 e^{-t/\tau_p}. \quad (5)$$

They can be interpreted as follows. Equation (3) states that the signal $\Delta S_{\text{inst}}[r, t]$ is a superposition of the signals corresponding to the electronic states X and Y . The short-lived electronic state Z does not contribute to the signal on the time scales under consideration. On the other hand, according to Eq. (4b), the laser-excited A_2 contracts in the state Y intimes comparable to τ_v . According to Eqs. (5), the population relaxation of A_2 between the states Y and X is exponential with a characteristic time τ_p . As said above, this process is assumed to be much slower than the contraction of A_2 in the state Y . Unfortunately, as simple as the above $\Delta S_{\text{inst}}[r, t]$ may be, it does not lead to a simple analytical expression for

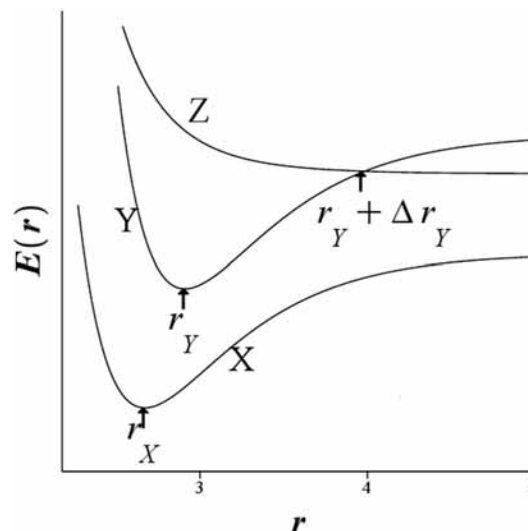


Fig. 2. Electronic energy surfaces of the molecule A_2 . The states X and Y are attractive, whereas the state Z is repulsive. The equilibrium A – A distance is r_X in the state X , and r_Y in the state Y . The energy surfaces of Y and Z cross each other at an A – A separation equal to $r_Y + \Delta r_Y$. To make a crossing possible, the Y and Z states must have different symmetries. This crossing is supposed to be infinitely fast in the present model

$\Delta S_{\text{inst}}(q, t)$. To avoid additional uncertainties, we prefer to use the well-known exact relation, which connects $\Delta S_{\text{inst}}(q, t)$ and $\Delta S_{\text{inst}}[r, t]$ [16]:

$$\Delta S_{\text{inst}}(q, t) = (4\pi/q) \int dr r \Delta S_{\text{inst}}[r, t] \sin(qr). \quad (6)$$

The function $\Delta S_{\text{inst}}(q, t)$ was then determined numerically.

D. The parameters of the above model were given as follows [13–15, 17, 18]: the equilibrium A – A distance r_X is 2.5 Å, and r_Y is 3.0 Å, whereas the laser-induced extension Δr_y in the state Y is 1.5 Å. In turn, the parameters a_X and a_Y are 10 Å⁻², which corresponds to a half-width of $g_X(r, t)$ and $g_Y(r, t)$ of the order of 0.3 Å. Moreover, the recombination time τ_v of the molecule A_2 in its electronic state Y is taken to be 100 ps, whereas the lifetime τ_p of this state is supposed to be 1000 ps. These values of parameters will be maintained throughout this work. Only the form of the incident X-ray pulse will vary from one calculation to another.

E. This above model represents, in fact, a simplified version of that employed one to analyze the recombination of the laser-dissociated I_2/CCl_4 or Br_2/CCl_4 solutions [9–11]. The main difference between them is that the A – A recombination is monoexponential here, whereas it was multiexponential in I_2/CCl_4 . Moreover, the solvent cage problems of I_2/CCl_4 are avoided, by

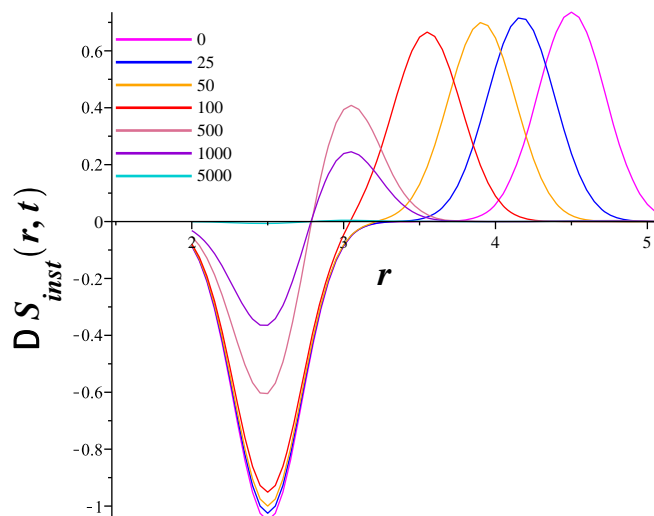


Fig. 3. Deconvoluted x-ray signals $\Delta S_{\text{inst}}[r, t]$, free of any instrumental deformation. They are presented for distances r such that $2 \text{ \AA} < r < 5 \text{ \AA}$ and for several times t taken in the interval $0 \text{ ps} < t < 5000 \text{ ps}$. The contraction of the laser-excited A_2 is clearly visible on the positive peak of $\Delta S_{\text{inst}}[r, t]$, which shifts gradually from 4.5 \AA to 3 \AA . Its negative peak around 2.5 \AA is due to the laser-generated hole in the ground-state population of A_2

imposing a potential energy curve crossing at $r_Y + \Delta r_Y$ to A_2 (Fig. 2). The characteristic times are also chosen similarly in both models; the present model is thus close to the physical reality. The convolution problems can be studied safely in its frame.

4. Non-Distorted Signals $\Delta S_{\text{inst}}[r, t]$ and $\Delta S_{\text{inst}}(q, t)$

The r -space signals $\Delta S_{\text{inst}}[r, t]$, free of any instrumental deformation, are presented first for $2 \text{ \AA} < r < 5 \text{ \AA}$ and $0 < t < 5000 \text{ ps}$ (Fig. 3). They are vanishing at negative times as expected. This is a consequence of the causality principle: the consequence cannot precede the cause. These signals appear firstly at $t = 0$ and exhibit two peaks. The positive peak at $r = 4.5 \text{ \AA}$ shows the presence of laser excited molecules A_2 in an extended configuration of the state Y , where $r = r_Y + \Delta r_Y$. The negative peak at $r = 2.5 \text{ \AA}$ indicates that the molecules promoted to the state Y are missing in the state X . At longer times, the positive peak shifts progressively from 4.5 \AA to 2.5 \AA , monitoring the contraction of the photoelongated A_2 in this way. Simultaneously, the negative peak at $r = 2.5 \text{ \AA}$ diminishes in its absolute value and vanishes in a few thousands of ps, when the thermal equilibrium is reestablished. This is how the return of a

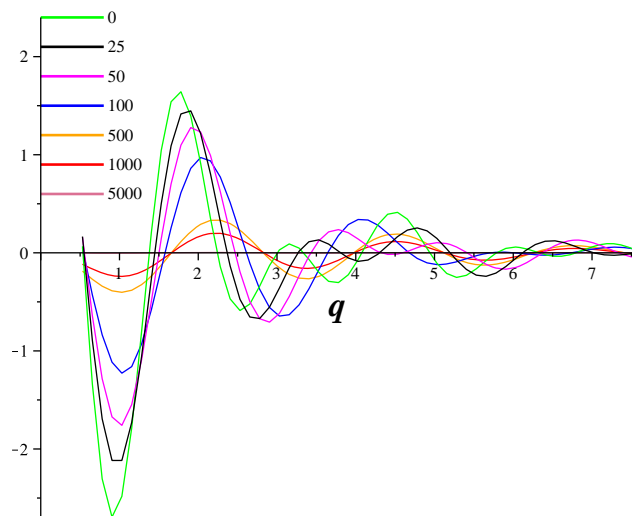


Fig. 4. Deconvoluted x-ray signals $\Delta S_{\text{inst}}(q, t)$ free of any instrumental deformation. They are presented for wave vectors q such that $0.5 \text{ \AA}^{-1} < q < 7 \text{ \AA}^{-1}$ and for several times t taken in the interval $0 \text{ ps} < t < 5000 \text{ ps}$. The contraction of the laser-excited A_2 manifests itself by high q shifts of both signal maxima and minima. However, the variation of the signals $\Delta S_{\text{inst}}(q, t)$ is less prominent than that of $\Delta S_{\text{inst}}[r, t]$

laser-excited solution to the thermal equilibrium manifests itself in an ideal x-ray diffraction experiment.

The q -space signals $\Delta S_{\text{inst}}(q, t)$ are presented next for a domain, where $0.50 \text{ \AA}^{-1} < q < 7 \text{ \AA}^{-1}$ and $0 < t < 5000 \text{ ps}$ (Fig. 4). The calculated curves exhibit damped oscillations. Signals $\Delta S_{\text{inst}}(q, t)$ cross the q -axis at the points q_n such that $\Delta q = q_{n+1} - q_n \sim \pi/r_Z$; here, r_Z is a distance somewhere between r_X and $r_Y + \Delta r_Y$. The intensity of $\Delta S_{\text{inst}}(q, t)$ decreases with time t ; simultaneously, the peaks shift to higher values of q . This is expected, as the high q shifts correspond to a contraction of the A - A distance. However, they are comparatively small and do not exceed 0.6 \AA^{-1} in our calculation. One concludes that q -space signals are less convenient to monitor the molecular dynamics than r -space signals.

5. Role of Duration of Probing X-ray Pulses

A. The influence of the x-ray pulse duration on the shape of a measured x-ray signal is the central point of the present study. The incident x-ray pulses $I_x(t - \tau)$ will be written as a Gaussian centered at the time τ , which is by no means a heavy restriction. Then $I_x(t - \tau) = I_0 \exp[-\alpha(t - \tau)^2]$, where I_0 is the amplitude of the x-ray pulse and α determines its duration.

B. The effect of x-ray pulses of finite duration is studied now. The functions $I_X(t - \tau)$ and $\Delta S_{\text{inst}}[r, t]$ are con-

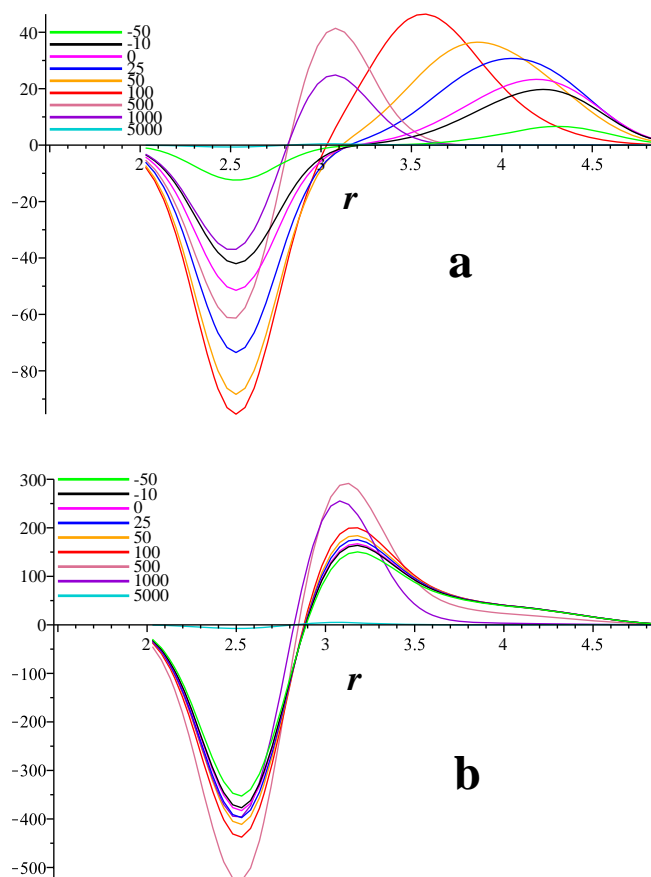


Fig. 5. Signals $\Delta S[r, \tau]$ calculated for x-ray pulses of finite width. They are presented for distances r such that $2 \text{ \AA} < r < 5 \text{ \AA}$ and for several pump-probe delays τ taken in the interval $-50 \text{ ps} < \tau < 5000 \text{ ps}$. The x-ray pulse duration is 100 ps in Fig. 5, a and 1000 ps in Fig. 5, b. The contraction of A_2 is clearly visible with x-ray pulses of 100 ps duration, but no longer for pulses of 1000 ps duration

volved to achieve this goal; the resulting signal $\Delta S[r, \tau]$ then corresponds to the experimental signal. This calculation was realized for $A-A$ separations r in the interval $2 \text{ \AA} < r < 5 \text{ \AA}$, and pump-probe time delays τ in the interval $-50 \text{ ps} < \tau < 5000 \text{ ps}$. The results are illustrated in Figs. 5, a, b; the following remarks are worth noting. In Fig. 5, a, the duration $\Delta\tau_{1/2}$ of the x-ray probe is the same as the time τ_v of contraction of the $A-A$ bond; one has $\Delta\tau_{1/2} = \tau_v = 100 \text{ ps}$. Under these conditions, the signals $\Delta S_{\text{inst}}[r, t]$ and $\Delta S[r, t]$ are similar to each other; compare Figs. 3 and 5, a. However, the similarity does not mean the identity. For example, the band intensities are smaller here than the true band intensities. This similarity disappears in Fig. 5, b, where $\Delta\tau_{1/2} = 1000 \text{ ps}$ and $\tau_v = 100 \text{ ps}$. In fact, if the x-ray pulse duration $\Delta\tau_{1/2}$ is long as compared to the contraction time τ_v ,

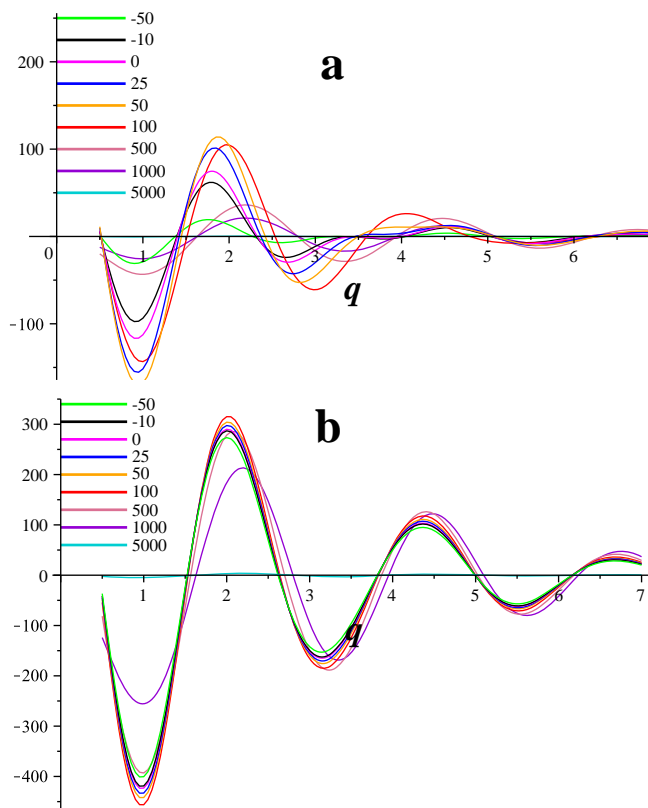


Fig. 6. Signals $\Delta S(q, \tau)$ calculated for x-ray pulses of finite width. They are presented for wave vectors q such that $0.5 \text{ \AA}^{-1} < q < 7 \text{ \AA}^{-1}$ and for several pump-probe delays τ taken in the interval $-50 \text{ ps} < \tau < 5000 \text{ ps}$. The x-ray pulse duration is 100 ps in Fig. 6, a and 1000 ps in Fig. 6, b. The contraction of the laser-excited A_2 manifests itself by high q shifts of both signal maxima and minima. However, this effect is hardly detectable at 1000 ps

this probing pulse mainly monitors contracted molecules A_2 . This contraction process can only be “filmed” with x-ray pulses of duration $\Delta\tau_{1/2}$ comparable to or shorter than τ_v . On the contrary, the slow population relaxation remains observable with longer pulses. This “collapse” of an x-ray signal, when the duration of probing x-ray pulses increases, is a novelty for time-resolved x-ray physics. However, it is not a novelty for general physics. In fact, a similar effect was observed and was carefully analyzed long time ago in NMR and in optics. It is well known under the name of motional narrowing; see, e.g., [19].

C. A similar study was realized in the q -space. The functions $I_X(t - \tau)$ and $\Delta S_{\text{inst}}(q, t)$ were convoluted to generate $\Delta S(q, \tau)$. The calculations were realized for wave vectors q between $0.50 \text{ \AA}^{-1} < q < 7 \text{ \AA}^{-1}$ and for pump-probe time delays τ in the interval $-50 \text{ ps} < \tau < 5000 \text{ ps}$. The results are illustrated in Figs. 6, a, b. The

times $\Delta\tau_{1/2}$ and τ_v are the same in Fig. 6, *a*, whereas $\Delta\tau_{1/2} \gg \tau_v$ in Fig. 6, *b*. One finds that, when $\Delta\tau_{1/2} = \tau_v$, the signals $\Delta S(q, \tau)$ of Fig. 6, *a* and $\Delta S_{\text{inst}}(q, t)$ of Fig. 4 are similar to each other, except for some blurring. In particular, the high q -shifts remain observable at short τ 's. This is less and less true for the signals $\Delta S(q, \tau)$ of Fig. 6, *b*, where $\Delta\tau_{1/2} \gg \tau_v$; dynamical effects are smaller in this case. The explanation of these findings is the same for $\Delta S[r, \tau]$. One concludes here again that r -resolved signals $\Delta S[r, \tau]$ are preferable for monitoring the molecular dynamics to q -resolved signals $\Delta S(q, \tau)$.

6. Improper Location of the Origin of X-Ray Pulses

We shall finally explore briefly the effect of an insufficiently precise temporal location of the probing x-ray pulse. The problem is not necessarily academic. A finite temporal width of probing x-ray pulses makes the measure of pump-probe time delays τ uncertain. In what follows, the laser pump pulse will be supposed to peak at the time $t = 0$, precisely. On the contrary, the x-ray pulses will peak at a time τ_0 which is not entirely under control. These pulses will be written as $I_X = I_0 \exp[-\alpha(t + \tau_0 - \tau)^2]$, where τ_0 denotes the incompletely controlled increment of the pump-probe time delay. In what follows, the quantity $\Delta\tau = \tau - \tau_0$ will be supposed to exhibit a Gaussian distribution $P(\Delta\tau) = (\beta/\pi)^{1/2} \exp[-(\Delta\tau)^2]$ in a given campaign of experiments; it may vary from one campaign to another. The signals $\Delta S[r, \tau]$, $S(q, \tau)$ must thus be averaged over all possible realizations of the x-ray probe fields. Then, designating this averaged x-ray pulse intensity by $\langle I_x(t - \tau) \rangle$, we obtain

$$\Delta S[r, \tau] = \int dt \langle I_x(t - \tau) \rangle \Delta S_{\text{inst}}[r, t],$$

$$\Delta S(q, \tau) = \int dt \langle I_x(t - \tau) \rangle \Delta S_{\text{inst}}(q, t), \quad (7)$$

where

$$\langle I_x(t - \tau) \rangle = (\beta/\pi)^{1/2} I_0 \times$$

$$\times \int d\Delta\tau \exp[-\alpha(t - \tau - \Delta\tau)^2] \exp[-\beta\Delta\tau^2] =$$

$$= [\beta/\alpha + \beta]^{1/2} I_0 \exp(-[\alpha\beta/(\alpha + \beta)](t - \tau)^2). \quad (8)$$

It results from the above analysis that the fluctuations of the pump-probe time delay can be accounted

for by simply replacing the true x-ray probe pulse shape $I_0 \exp[-\alpha(t - \tau)^2]$ by the effective x-ray pulse shape given by Eq. (8). This results in a small intensity change in the diffracted signal and a small broadening. The effects are rarely spectacular. For example, if the jitter in the pump-probe time delays amounts to 20% of the nominal temporal half-width of the probing x-ray pulse of 100 ps, the width of the effective x-ray pulse increases only by 2 ps. If this spread is of 50%, the effective pulse broadens for approximately 10 ps. We do not believe that the Gaussian approximation affects the above results to any considerable extent.

7. Conclusions

Convolution problems are omnipresent in natural sciences. They also play an important role in spectroscopy and in time-resolved x-ray diffraction. Finite slit width problems of the first of these two techniques are replaced by those of finite x-ray pulse duration in the second. Deconvolution techniques, needed to improve the experimental resolution, are similar in both these fields. The motional narrowing of spectral bands, well known in NMR and in optics, is present in x-ray diffraction too. It forbids visualizing the atomic motions during a chemical reaction, if x-ray pulses are not short enough. It should finally be noted that the convolution problems well-known in spectroscopy over many years are new in x-ray physics.

This paper may be concluded, by reproducing the well-known statement, which remains more than ever of actuality (20): "Would you rather use the deconvolution or build a more highly resolving instrument? Generally, this is not a well-posed question. However, the answer, if both time and resources are unlimited, is to build a better instrument. If not, the deconvolution should be applied".

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ЗАДАЧІ КОНВОЛЮЦІЇ ДЛЯ ДИФРАКЦІЇ
РЕНТГЕНІВСЬКИХ ПРОМЕНІВ
З ЧАСОВИМ РОЗРІЗНЕННЯМ

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Резюме

Теоретично досліджено задачі конволюції для розсіяння рентгенівських променів з тривалістю імпульсів 10–1000 пс. У ролі модельної системи вибрано розбавлену суміш діатомних молекул A_2 в інертному розріджувачі. Система опромінюється субпікосекундними імпульсами лазера, що переводять молекули A_2 в збуджений стан. При поверненні в основний стан молекула проходить через декілька проміжних станів. У рамках цієї моделі вивчено залежність різних рентгенівських сигналів від тривалості тестуючих рентгенівських імпульсів. Спочатку досліджено незміщені сигнали, які генеровані дуже короткими рентгенівськими імпульсами. При цьому чітко видно зміни геометрії молекул по r -розрізнених сигналах, і вони менше помітні при q -розрізненні. Потім вивчено сигнали, що генеровані рентгенівськими імпульсами скінченної тривалості. Рух атомів залишається помітним, якщо рентгенівські імпульси коротші чи порівнянні по тривалості з часом молекулярної динаміки. Тут також r -розрізнений сигнал більше підходить для моніторингу молекулярної динаміки, ніж q -розрізнені сигнали. Крім того, вивчено ефект недостатньої часової локалізації тестуючих рентгенівських імпульсів у порівнянні зі збуджуючими імпульсами лазера. Показано, що цей останній ефект може бути пояснений простою заміною реальної інтенсивності рентгенівського імпульсу іншою, теоретично передбачуваною інтенсивністю. Підкреслено схожість методів деконволюції у спектроскопії та у дифракції рентгенівських променів з часовим розрізненням.