

## Multicriteria problem of evaluation of the enterprise labor protection management system efficiency

Olyanyshen T. V.<sup>1</sup>, Storozhuk V. M.<sup>1</sup>, Yatsiuk R. A.<sup>2</sup>, Korzh H. I.<sup>2</sup>, Ratushniak Yu. V.<sup>3</sup>,  
Melnikov A. V.<sup>3</sup>

<sup>1</sup>*National University of Forestry and Wood Technology,  
103 General Chuprynka Str., 79057, Lviv, Ukraine*

<sup>2</sup>*Lviv Polytechnic National University,  
12 S. Bandera Str., 79013, Lviv, Ukraine*

<sup>3</sup>*IT STEP University,  
83A Zamarstynivska Str., 79011, Lviv, Ukraine*

(Received 14 August 2020; Revised 17 March 2021; Accepted 20 April 2021)

Introduction of the system of enterprise labor protection management still remains a topical question for business entities of production and non-production activity spheres. The effectiveness evaluation of enterprise labor protection management is based on the method of multicriteria choice of alternatives using the fuzzy preference relations. The application of the chosen method allows, unlike the other methods, to identify its shortcomings in all objectivity detecting the adverse consequences. Therefore, the situation can be normalized in time.

**Keywords:** *labor protection management system, efficiency of system functioning, multicriteria choice of alternatives, fuzzy preference relations.*

**2010 MSC:** 03B52

**DOI:** 10.23939/mmc2021.02.330

### 1. Introduction

The labor protection management system (LPMS) is an effective tool that allows the business entity to ensure the appropriate level of labor protection at the enterprise, satisfying the necessary requirements to ensure safe and healthy working conditions for employees. The issue of LPMS implementation remains the relevant one for the subjects of productive and non-productive spheres of activity. The approaches to the construction and operation of LPMS are constantly improved, taking into account the international experience. In particular, using the risk-oriented approach, the principles, directions, and objectives of constructing a system of occupational safety and health in Ukraine are identified to create a national system preventing occupational risks and providing safe and healthy working conditions [1].

The issue of developing an effective LPMS is relevant for the domestic and foreign companies as well, as one can obviously see in the international regulations adopted at different times [2, 3]. A lot of publications, in particular, [4–9], are devoted to the formulation, optimization, and efficiency evaluation of LPMS problems.

### 2. Problem formulation

The issue of evaluating the effectiveness of LPMS can't been exhausted since there are different approaches to its solving, due to the characteristics of the business entity — production or non-production activities; the presence of facilities, equipment, high-risk work; features of production and technological processes; relationships within departments; number and training of staff, etc. The proposed approach to evaluate the effectiveness of LPMS of the enterprise is based on the method of multi-criteria choice of alternatives using the fuzzy preference relations [10–14]. There are the well-known examples of this method application to solve problems being related to the economic security of business entities [15–17].

The effectiveness of LPMS is modeled and studied basing on this approach. Also in the paper there is constructed and studied a mathematical model of LPMS operation for a specific enterprise in the chemical industry as an example. To solve the problem there is considered a method [12] basing on an algorithm for alternative's choice in the case of multi- criteria of optimality (fuzzy preference relations).

### 3. Algorithm description

Let on the universal set  $X$  of alternatives, the preference relations  $R_1, R_2, \dots, R_m$  (fuzzy or unfuzzy) with membership functions  $\mu_j(x, y)$  be given, as well as the weight coefficients  $\omega_j$  of the corresponding relations, where  $j = \overline{1, m}$ .

A convolution (composition) of fuzzy relations  $R_1, R_2, \dots, R_m$  in the form of meet of sets ( $Q_1 = \cap_{j=1}^m R_j$ ), with the membership function is constructed as:

$$\mu_{Q_1}(x_i, x_j) = \min \{ \mu_{R_1}(x_i, x_j), \mu_{R_2}(x_i, x_j), \dots, \mu_{R_m}(x_i, x_j) \}. \tag{1}$$

Determine the set of non-dominant alternatives  $Q_1^{nd}$  in the set  $(X, Q_1)$ :

$$\begin{aligned} \mu_{Q_1}^s(x_i, x_j) &= \max \{ 0; \mu_{Q_1}(x_i, x_j) - \mu_{Q_1}(x_j, x_i) \}, \\ \mu_{Q_1}^{nd}(x) &= 1 - \max \mu_{Q_1}^s(x_i, x_j). \end{aligned} \tag{2}$$

Using the convolution of criteria in the form of the sum (give definition), one can construct a fuzzy preference relation  $Q_2$  in the next form:

$$\mu_{Q_2}(x_i, x_j) = \sum_{j=1}^m \omega_j \mu_{R_j}(x_i, x_j), \quad \sum_{j=1}^m \omega_j = 1, \quad \omega_j \geq 0. \tag{3}$$

Obtaining a fuzzy subset of non-dominant alternatives by means of  $Q_2$ , there is constructed a membership function

$$\begin{aligned} \mu_{Q_2}^s(x_i, x_j) &= \max \{ 0; \mu_{Q_2}(x_i, x_j) - \mu_{Q_2}(x_j, x_i) \}, \\ \mu_{Q_2}^{\bar{A}}(x) &= 1 - \max \mu_{Q_2}^s(x_j, x_i). \end{aligned} \tag{4}$$

Having found the meet of sets  $Q_1^{nd}, Q_2^{nd}$  and the common set of non-dominant alternatives  $Q_{nd} = Q_1^{nd} \cap Q_2^{nd}$  with the membership function

$$\mu_{Q_{nd}}^{nd}(x) = \min \{ \mu_{Q_1}^{nd}(x), \mu_{Q_2}^{nd}(x) \} \tag{5}$$

a choice of alternatives can be derived from the set  $X_{chnd}$ :

$$X_{chnd} = \left\{ x^* : \mu_{nd}(x^*) = \sup_x \mu_{nd}(x), x \in X \right\}. \tag{6}$$

We will consider the choice of alternatives from the set  $X_{chnd}$  with the greatest degree of non-dominance to be the best one.

### 4. Modeling of LPMS efficiency of the enterprise with application of the suggested algorithm

Using the results [18], consider the following threats related to the activities of the labor protection service, which may adversely affect the effectiveness of LPMS (alternatives,  $x_i$ ):  $x_{25}$  is a low level of visual agitation on occupational safety;  $x_{26}$  is a non-compliance with current requirements for record keeping on labor protection;  $x_{27}$  is a failure to implement the planned activities in a timely manner;  $x_{28}$  is a non-compliance with the labor protection regulations in a timely manner;  $x_{29}$  is the control periodicity violation over the state of labor protection in the structural units;  $x_{30}$  is an excess of the injury frequency at the enterprise over their frequency in the industry;  $x_{31}$  is an excess of the injury severity at the enterprise over their severity in the industry;  $x_{32}$  is a failure to comply with the measures

provided for in the acts of the accident investigation in a timely manner;  $x_{33}$  is an unpreparedness of the labor protection personnel;  $x_{34}$  is the violation of the briefing frequency, certification and re-certification of the occupational safety;  $x_{35}$  is gross violation of occupational safety rules, accidents;  $x_{36}$  is non-use of personal protective equipment and overalls by workers;  $x_{37}$  is the level of provision with the domestic premises;  $x_{38}$  is the unscheduled implementation of measures to improve working conditions;  $x_{39}$  is the implementation of proposals to improve working conditions. Each alternative reflects a different degree of impact on the effectiveness of LPMS.

According to the criteria  $R_j$ , the choice is made among the identified alternatives (threats) that may adversely affect the effectiveness of LPMS:  $R_1$  stands for the threat occurs infrequently and irregularly;  $R_2$  is the appearance of a threat from time to time;  $R_3$  means the threat occurs frequently and regularly over a period of time.

To determine  $\omega_i$  (the weight of the  $i$ -th criterion) using the T. Saati's scale of relative importance of objects [19], let us form a matrix of paired comparisons of criteria (when the criterion located in the row is compared with all the criteria specified in the column of matrix), according to which the choice among threats to the effectiveness of LPMS is performed:

$$A = \begin{pmatrix} 1 & 1/7 & 1/9 \\ 7 & 1 & 1/3 \\ 9 & 3 & 1 \end{pmatrix}.$$

Using the algorithm [11–14, 19], one can obtain the weights of the criteria  $\omega_i$ , consequently the choice is made among the specified threats: threats that occur infrequently and irregularly  $\omega_1 = 0.054$ ; occurrence of a threat from time to time  $\omega_2 = 0.289$ ; threats that occur frequently and regularly (recurrence of the threat) over a period of time  $\omega_3 = 0.655$ ,  $\sum_{i=1}^n \omega_i = 1$ . The consistency index of the matrix of pairwise comparisons  $A$  is within the norm ( $\leq 0.1$ ), i.e. we get satisfactory results of comparisons.

The threats were compared according to all relations in the  $R_j$  criteria, so they could adversely affect the effectiveness of LPMS. The results were evaluated by the membership function:

$$\mu_R(x_i, x_j) = \begin{cases} 1, & \text{if } x_i \succ x_j \text{ or } x_i \approx x_j, \\ 0, & \text{if } x_i \prec x_j \end{cases} \quad (7)$$

where  $x_i, x_j$  are threats related to the activities of the labor protection service, that can adversely affect the effectiveness of LPMS.

From Eq. (7) one can see that if one threat prevails or is equal to another, in the corresponding matrix cell would be 1, if it is  $\prec$  1 in the matrix cell would be 0. Construct a matrix of relations  $\mu_{R_j}(x_i, x_j)$  (Tables 1–3).

A convolution of the relations  $R_1, R_2, R_3$  is constructed in the form of meet of sets  $Q_1 = R_1 \cap R_2 \cap R_3$  with the membership function  $\mu_{Q_1}(x_i, x_j)$  (1). The results are presented in the Table A.1.

Results of the ratio of strict preference  $Q_1^S$  (results of  $\mu_{Q_1}^S(x_i, x_j)$  calculations by formula (2) are presented in the Table A.2.

The set of non-dominant alternatives  $Q_1^{nd}$  is determined in the set  $(X, Q_1)$ , and the membership function  $\mu_{Q_1}^{nd}(x)$  is constructed in the following form:

$$\mu_{Q_1}^{nd}(x) = [0; 0; 0; 0; 0; 1; 1; 0; 0; 0; 1; 0; 0; 0; 0].$$

There is calculated the fuzzy preference relation  $Q_2 = \sum_{j=1}^m \omega_j f_j(x)$  and its membership function  $\mu_{Q_2}(x_i, x_j) = \sum_{k=1}^3 \omega_k \mu_{R_k}(x_i, x_j)$ . The results of calculations under the condition (3) are presented in the Table A.3).

Taking into account the ratio of the strict preference by the second convolution  $Q_2^S$ , the membership function  $\mu_{Q_2}^S(x_i, x_j)$  is constructed by Eq. (4), and the calculation results are presented in the Table A.4.

Determine the non-dominant alternatives by the second convolution  $Q_2^{nd}$  and construct the membership function  $\mu_{Q_2}^{nd}(x)$ :

**Table 1.** Relationship matrix  $\mu_{R_1}(x_i, x_j)$ .

$x_i/x_j$	$x_{25}$	$x_{26}$	$x_{27}$	$x_{28}$	$x_{29}$	$x_{30}$	$x_{31}$	$x_{32}$	$x_{33}$	$x_{34}$	$x_{35}$	$x_{36}$	$x_{37}$	$x_{38}$	$x_{39}$
$x_{25}$	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
$x_{26}$	1	1	1	1	1	0	0	1	0	1	0	1	0	1	1
$x_{27}$	1	0	1	1	1	0	0	0	0	1	0	0	0	1	1
$x_{28}$	1	0	0	1	1	0	0	0	1	1	0	1	1	1	1
$x_{29}$	1	0	0	0	1	0	0	0	1	1	0	1	1	1	1
$x_{30}$	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1
$x_{31}$	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
$x_{32}$	1	0	1	1	1	0	0	1	1	1	0	1	1	1	1
$x_{33}$	1	1	1	0	0	0	0	0	1	1	1	0	0	1	1
$x_{34}$	1	0	0	0	0	0	0	0	0	1	0	1	1	1	1
$x_{35}$	1	1	1	1	1	0	0	1	0	1	1	1	1	1	1
$x_{36}$	1	0	1	0	0	0	0	0	1	0	0	1	1	1	1
$x_{37}$	1	1	1	0	0	0	0	0	1	0	0	0	1	0	1
$x_{38}$	1	0	0	0	0	0	0	0	0	0	0	0	0	1	1
$x_{39}$	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1

**Table 2.** Relationship matrix  $\mu_{R_2}(x_i, x_j)$ .

$x_i/x_j$	$x_{25}$	$x_{26}$	$x_{27}$	$x_{28}$	$x_{29}$	$x_{30}$	$x_{31}$	$x_{32}$	$x_{33}$	$x_{34}$	$x_{35}$	$x_{36}$	$x_{37}$	$x_{38}$	$x_{39}$
$x_{25}$	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
$x_{26}$	1	1	1	1	1	0	0	0	1	1	0	1	1	1	1
$x_{27}$	1	0	1	0	0	0	0	0	1	0	0	0	0	1	1
$x_{28}$	1	0	1	1	0	0	0	1	1	1	0	0	0	1	1
$x_{29}$	1	0	1	1	1	0	0	1	1	1	0	0	0	1	1
$x_{30}$	1	1	1	1	1	1	0	1	1	1	0	1	1	1	1
$x_{31}$	1	1	1	1	1	1	1	0	0	0	0	1	1	1	1
$x_{32}$	1	1	1	0	0	0	1	1	1	1	0	1	1	1	1
$x_{33}$	1	0	0	0	0	0	1	0	1	1	0	1	1	1	1
$x_{34}$	1	0	1	0	0	0	1	0	0	1	1	1	1	1	1
$x_{35}$	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
$x_{36}$	1	0	1	1	1	0	0	0	0	0	0	1	1	1	1
$x_{37}$	1	0	1	1	1	0	0	0	0	0	0	0	1	1	1
$x_{38}$	1	0	0	0	0	0	0	0	0	0	0	0	0	1	1
$x_{39}$	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1

**Table 3.** Relationship matrix  $\mu_{R_3}(x_i, x_j)$ .

$x_i/x_j$	$x_{25}$	$x_{26}$	$x_{27}$	$x_{28}$	$x_{29}$	$x_{30}$	$x_{31}$	$x_{32}$	$x_{33}$	$x_{34}$	$x_{35}$	$x_{36}$	$x_{37}$	$x_{38}$	$x_{39}$
$x_{25}$	1	1	1	1	1	0	0	0	0	0	0	1	1	1	1
$x_{26}$	0	1	1	1	1	1	1	1	1	1	0	1	1	1	1
$x_{27}$	0	0	1	1	1	0	0	1	1	1	0	1	1	1	1
$x_{28}$	0	0	0	1	1	0	0	1	1	1	0	1	1	1	1
$x_{29}$	0	0	0	0	1	0	0	1	1	0	0	1	1	1	1
$x_{30}$	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1
$x_{31}$	1	0	1	1	1	0	1	1	1	1	1	1	1	1	1
$x_{32}$	1	0	0	0	0	0	0	1	1	1	1	1	1	1	1
$x_{33}$	1	0	0	0	0	0	0	0	1	1	1	1	1	1	1
$x_{34}$	1	0	0	0	1	0	0	0	0	1	1	1	1	1	1
$x_{35}$	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1
$x_{36}$	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1
$x_{37}$	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1
$x_{38}$	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
$x_{39}$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

$$\mu_{Q_2}^{nd}(x) = [0; 0.112; 0; 0; 0; 0.112; 0; 0; 0; 0.112; 0.690; 0; 0; 0; 0].$$

It is found a common set of the non-dominant alternatives by both convolutions  $Q^{nd}(X) = Q_1^{nd}(X) \cap Q_2^{nd}(X)$  with the membership function  $\mu_Q^{nd}(x)$  by the equality (5):

$$\mu_Q^{nd}(x) = [0; 0; 0; 0; 0; 0.112; 0; 0; 0; 0; 0.690; 0; 0; 0; 0].$$

According to the dependence (6), the most important alternative should be considered as one with the maximum degree of non-dominance for both convolutions. The obtained results show that the most significant threats to the effectiveness of LPMS of the analyzed enterprise are  $x_{30}$ , namely the exceeding injury frequency at the enterprise over their frequency in the industry and  $x_{35}$ , that is gross violation of occupational safety rules, accidents.

## 5. Conclusions

The obtained simulation results indicate that an accident has occurred or may occur at the assessed enterprise. The application of the method of multi-criteria choice of alternatives based on fuzzy preference relations in the process of evaluating the LPMS effectiveness, considered in this paper, allows, unlike a lot of other methods, to obtain more objective identification of LPMS shortcomings which could potentially lead to undesirable consequences and, accordingly, to take the necessary measures in time to normalize the situation.

- 
- [1] Postanova Kabinetu Ministriv Ukrainy vid 12.12.2018 №989-p. Pro skhvalennia Kontseptsii reformuvannia systemy upravlinnia okhoronoiu pratsi v Ukraini ta zatverdzhennia planu zakhodiv shchodo yii realizatsii. <https://zakon.rada.gov.ua/laws/show/989-2018-%D1%80#Text> (in Ukrainian).
  - [2] Guidelines on occupational safety and health management systems: ILO-OSH 2001.
  - [3] DSTU ISO 45001:2019. Systemy upravlinnia okhoronoiu zdorovia ta bezpekoiu pratsi. Vymohy ta nastanovy shchodo zastosuvannia (ISO 45001:2018, IDT). [http://online.budstandart.com/ua/catalog/doc-page.html?id\\_doc=88004](http://online.budstandart.com/ua/catalog/doc-page.html?id_doc=88004) (in Ukrainian).
  - [4] Gogitashvili G. G. Systemy upravlinnia okhoronoiu pratsi. Lviv, Afisha (2002), (in Ukrainian).
  - [5] Gogitashvili G. G., Karchevski E. T., Lapin V. M. Management of labor protection and risk according to international standards. Kyiv, Znannia (2007), (in Ukrainian).
  - [6] Storozhuk V. M. Otsiniuvannia ta kontrol bezpechnosti promysloвого pidpryemstva. Nauk. visn. NLTU Ukrainy. **25** (2), 157–161 (2015), (in Ukrainian).
  - [7] Gogitashvili G. G., Lapin V. M., Yatsiuk R. A., Storozhuk V. M., Melnikov A. V. Osnovy okhorony pratsi. Kyiv, Znannia (2016), (in Ukrainian).
  - [8] Storozhuk V. M., Melnikov A. V., Yatsiuk R. A. Osoblyvosti protsedury otsiniuvannia stanu bezpechnosti promysloвого pidpryemstva. Tekhnol. i tekhn. druzarstva. **3** (53), 35–48 (2016), (in Ukrainian).
  - [9] Storozhuk V. M., Olyanyshen T. V., Melnikov A. V., Yatsiuk R. A. Otsiniuvannia ryzykiv na robochomu misti, yak element ryzykooorientovanoho pidkhodu v okhoroni pratsi. Tekhnol. i tekhn. druzarstva. **1** (63), 35–44 (2019), (in Ukrainian).
  - [10] Bellman R., Zade L. Prinyatie resheniy v rasplyvchatyih usloviyah. Voprosy analiza i protsedury prinyatiya resheniy. Moskva, Mir (1976), (in Russian).
  - [11] Zade L. Ponyatie lingvisticheskoy peremennoy i ego primenenie k prinyatiyu priblizhennyih resheniy. Moskva, Mir (1976), (in Russian).
  - [12] Zaichenko Yu. P. Yssledovanye operatsyi. Kiev, Slovo (2006), (in Russian).
  - [13] Kostrobii P. P., Ryzha I. A. Matematyчне modeliuвання v umovakh nevyznachenosti. Lviv, Rastr-7 (2018), (in Ukrainian).
  - [14] Raskin L. G., Seraya O. V. Nechetkaya matematika. Osnovy teorii. Prilozheniya. Kharkov, Parus (2008), (in Russian).

- [15] Zhyvko Z. B. Metodolohiia upravlinnia ekonomichnoiu bezpekoiu pidpriemstva. Lviv, Liha-Pres, 359–374 (2013), (in Ukrainian).
- [16] Melnikov A. V., Karaim M. M. Bahatofaktornyi vybir alternatyvnykh variantiv optymalnoho antykryzovoho rishennia v protsesi harantuvannia ekonomichnoi bezpeky pidpriemstva na osnovi nechitkoho vidnoshennia perevahy. Nauk. visn. NLTU Ukrainy. **23** (3), 355–362 (2013), (in Ukrainian).
- [17] Karaim M. M., Martyniv V. V., Shtanhret A. M., Kotlyarevsky Ya. V., Sukhomlyn L. Ye., Ratushniak Yu. V. Antykryzovi tekhnolohii v upravlinni ekonomichnoiu bezpekoiu pidpriemstva. Lviv, Ukr. akad. drukarstva. 132–142 (2016), (in Ukrainian).
- [18] Storozhuk V. M., Dzhyhyrei V. S., Sokolovskiy I. A. Okhorona pratsi ta promyslova ekolohiia v haluzi: Praktykum z dystsypliny. Lviv, NLTUU (2006), (in Ukrainian).
- [19] Saaty T. Pryniatye reshenyi. Metod analiza yerarkhyi: per. s anhl. Moskva, Radyo i sviaz (1993), (in Russian).

## Appendix

**Table A.1.** Relationship matrix  $\mu_{Q1}(x_i, x_j)$ .

$x_i/x_j$	$x_{25}$	$x_{26}$	$x_{27}$	$x_{28}$	$x_{29}$	$x_{30}$	$x_{31}$	$x_{32}$	$x_{33}$	$x_{34}$	$x_{35}$	$x_{36}$	$x_{37}$	$x_{38}$	$x_{39}$
$x_{25}$	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
$x_{26}$	0	1	1	1	1	0	0	0	0	1	0	1	0	1	1
$x_{27}$	0	0	1	0	0	0	0	0	0	0	0	0	0	1	1
$x_{28}$	0	0	0	1	0	0	0	0	1	1	0	0	0	1	1
$x_{29}$	0	0	0	0	1	0	0	0	1	0	0	0	0	1	1
$x_{30}$	1	0	1	1	1	1	0	1	1	1	0	1	1	1	1
$x_{31}$	1	0	1	1	1	0	1	0	0	0	0	1	1	1	1
$x_{32}$	1	0	0	0	0	0	0	1	1	1	0	1	1	1	1
$x_{33}$	1	0	0	0	0	0	0	0	1	1	0	0	0	1	1
$x_{34}$	1	0	0	0	0	0	0	0	0	1	0	1	1	1	1
$x_{35}$	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1
$x_{36}$	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1
$x_{37}$	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1
$x_{38}$	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
$x_{39}$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

**Table A.2.** Matrix  $\mu_{Q1}^s(x_i, x_j)$ .

$\mu_{Q1}^s(x_i, x_j)$	$x_{25}$	$x_{26}$	$x_{27}$	$x_{28}$	$x_{29}$	$x_{30}$	$x_{31}$	$x_{32}$	$x_{33}$	$x_{34}$	$x_{35}$	$x_{36}$	$x_{37}$	$x_{38}$	$x_{39}$
$x_{25}$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
$x_{26}$	0	0	1	1	1	0	0	0	0	1	0	1	0	1	1
$x_{27}$	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1
$x_{28}$	0	0	0	0	0	0	0	0	1	1	0	0	0	1	1
$x_{29}$	0	0	0	0	0	0	0	0	1	0	0	0	0	1	1
$x_{30}$	1	0	1	1	1	0	0	1	1	1	0	1	1	1	1
$x_{31}$	1	0	1	1	1	0	0	0	0	0	0	1	1	1	1
$x_{32}$	1	0	0	0	0	0	0	0	1	1	0	1	1	1	1
$x_{33}$	1	0	0	0	0	0	0	0	0	1	0	0	0	1	1
$x_{34}$	1	0	0	0	0	0	0	0	0	0	0	1	1	1	1
$x_{35}$	1	1	1	1	1	0	0	0	0	0	0	1	1	1	1
$x_{36}$	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1
$x_{37}$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
$x_{38}$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
$x_{39}$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

**Table A.3.** Matrix  $\mu_{Q_2}(x_i, x_j)$ .

$\mu_{Q_2}(x_i, x_j)$	$x_{25}$	$x_{26}$	$x_{27}$	$x_{28}$	$x_{29}$	$x_{30}$	$x_{31}$	$x_{32}$	$x_{33}$	$x_{34}$	$x_{35}$	$x_{36}$	$x_{37}$	$x_{38}$	$x_{39}$
$x_{25}$	1	0.655	0.655	0.655	0.655	0	0	0	0	0	0	0.655	0.655	0.655	0.655
$x_{26}$	0.345	1	1	1	1	0.655	0.655	0.711	0.944	1	0	1	0.944	1	1
$x_{27}$	0.345	0	1	0.711	0.711	0	0	0.655	0.944	0.711	0	0	0	0.345	0.345
$x_{28}$	0.345	0	0.289	1	0.711	0	0	0.944	1	1	0	0.711	0.711	1	1
$x_{29}$	0.345	0	0.289	0.289	1	0.289	0	0.944	1	0.345	0	0.711	0.711	1	1
$x_{30}$	1	0.345	1	1	0.711	1	0.944	1	1	1	0.711	1	1	1	1
$x_{31}$	1	0.345	1	1	1	0.056	1	0.711	0.711	0.711	0.711	1	1	1	1
$x_{32}$	1	0.289	0.345	0.056	0.056	0	0.289	1	1	1	0.655	1	1	1	1
$x_{33}$	1	0.056	0.056	0	0	0	0.289	0	1	1	0.711	0.944	0.944	1	1
$x_{34}$	1	0	0.289	0	0.655	0	0.289	0	0	1	0.944	1	1	1	1
$x_{35}$	1	1	1	1	1	0.289	0.289	0.345	0.289	0.056	1	1	1	1	1
$x_{36}$	0.345	0	1	0.289	0.289	0	0	0	0.056	0	0	1	1	1	1
$x_{37}$	0.345	0.056	1	0.289	0.289	0	0	0	0.056	0	0	0	1	0.944	1
$x_{38}$	0.345	0	0.655	0	0	0	0	0	0	0	0	0	0.056	1	1
$x_{39}$	0.345	0	0.655	0	0	0	0	0	0	0	0	0	0	0	1

**Table A.4.** Matrix  $\mu_{Q_2}^s(x_i, x_j)$ .

$\mu_{Q_2}^s(x_i, x_j)$	$x_{25}$	$x_{26}$	$x_{27}$	$x_{28}$	$x_{29}$	$x_{30}$	$x_{31}$	$x_{32}$	$x_{33}$	$x_{34}$	$x_{35}$	$x_{36}$	$x_{37}$	$x_{38}$	$x_{39}$
$x_{25}$	0	0.310	0.310	0.310	0.310	0	0	0	0	0	0	0.310	0.310	0.310	0.310
$x_{26}$	0	1	1	1	1	0.310	0.310	0.422	0.888	1	0	1	0.888	1	1
$x_{27}$	0	0	0	0.422	0.422	0	0	0.310	0.888	0.422	0	0	0	0	0
$x_{28}$	0	0	0	0	0.422	0	0	0.888	1	1	0	0.422	0.422	1	1
$x_{29}$	0	0	0	0	0	0	0	0.888	1	0	0	0.422	0.422	1	1
$x_{30}$	1	0	1	1	0.422	0	0.888	1	1	1	0.422	1	1	1	1
$x_{31}$	1	0	1	1	1	0	0	0.422	0.422	0.422	0.422	1	1	1	1
$x_{32}$	1	0	0	0	0	0	0	0	1	1	0.310	1	1	1	1
$x_{33}$	1	0	0	0	0	0	0	0	0	1	0.422	0.888	0.888	1	1
$x_{34}$	1	0	0	0	0.310	0	0	0	0	0	0.888	1	1	1	1
$x_{35}$	1	1	1	1	1	0	0	0	0	0	0	1	1	1	1
$x_{36}$	0	0	1	0	0	0	0	0	0	0	0	0	1	1	1
$x_{37}$	0	0	1	0	0	0	0	0	0	0	0	0	0	0.888	1
$x_{38}$	0	0	0.310	0	0	0	0	0	0	0	0	0	0	0	1
$x_{39}$	0	0	0.310	0	0	0	0	0	0	0	0	0	0	0	0

## Багатокритеріальна задача оцінювання ефективності системи управління охороною праці підприємства

Олянишен Т. В.<sup>1</sup>, Сторожук В. М.<sup>1</sup>, Яцюк Р. А.<sup>2</sup>, Корж Г. І.<sup>2</sup>,  
Ратушняк Ю. В.<sup>3</sup>, Мельников О. В.<sup>3</sup>

<sup>1</sup>Національний лісотехнічний університет України,  
вул. Генерала Чупринки, 103, 79057, Львів, Україна

<sup>2</sup>Національний університет “Львівська політехніка”,  
вул. С. Бандери, 12, 79013, Львів, Україна

<sup>3</sup>ІТ СТЕП Університет,  
вул. Замарстинівська, 83А, 79011, Львів, Україна

Питання впровадження системи управління охороною праці підприємства впродовж багатьох років залишаються актуальним для суб'єктів господарювання виробничої та невиробничої сфер діяльності. У роботі оцінювання ефективності СУОП підприємства базується на застосуванні методу багатокритеріального вибору альтернатив на основі нечіткого відношення переваги. Застосування обраного методу дозволяє, на відміну від низки інших методів, більш об'єктивно виокремити її недоліки, які можуть призвести до небажаних наслідків і, відповідно, вчасно вжити необхідні заходи для нормалізації ситуації.

**Ключові слова:** система управління охороною праці, ефективність функціонування системи, багатокритеріальний вибір альтернатив, нечіткі відношення переваги.